

Obliczyć całki nieoznaczone:

1. [0,6 pkt]

$$\int \frac{\sin(2x)}{\sqrt{7 + 9 \sin^2(x)}} dx,$$

2. [0,6 pkt]

$$\int \frac{x^5 + 7x - 3}{(1 + x^2)(x - 4)} dx,$$

3. [0,6 pkt]

$$\int (3x^2 + 5x - 2)\sqrt{x^2 + 4x - 1} dx,$$

4. [0,6 pkt]

$$\int \frac{dx}{\sin(3x) \cos(x)},$$

5. [0,6 pkt]

$$\int \frac{2x + 3}{(4x^2 + 20x + 40)^3} dx.$$

Wskazówki:

$$(\arcsin x)' = \frac{1}{\sqrt{1 - x^2}},$$

$$(\arccos x)' = \frac{-1}{\sqrt{1 - x^2}},$$

$$(\operatorname{ar sinh} x)' = \frac{1}{\sqrt{1 + x^2}},$$

$$(\operatorname{ar cosh} x)' = \frac{1}{\sqrt{x^2 - 1}},$$

$$\sin^2(x) + \cos^2(x) = 1,$$

$$\cosh^2(x) - \sinh^2(x) = 1,$$

$$\sin(\arccos x) = \sqrt{1 - x^2},$$

$$\cos(\arcsin x) = \sqrt{1 - x^2}.$$