

## Tutorial 12

1. Prove that strong bisimulation equivalence allows for NFA (nondeterministic finite automata) minimization.
2. Suppose that  $P$  simulates  $Q$  and vice versa. Does it already mean that  $P$  is bisimilar to  $Q$ ?
3. Prove that  $P \sim Q$  iff Duplicator has a winning strategy from  $(P, Q)$ .
4. Can a modification of the bisimulation game be used to define the following relations:  $\approx, \sim_n, \approx_n, \sim_\omega, \sim_{\omega+1}, \preceq$  (simulation).
5. Prove that if  $S$  is a bisimulation up to  $\sim$ , then  $S \subseteq \sim$ .
6. Let  $X, Y$  be defined as follows:

$$\begin{array}{ll}
 P_1 \stackrel{\text{def}}{=} a_1.b_1.P_1 & Q_1 \stackrel{\text{def}}{=} a_1.\bar{p}.b_1.\bar{v}.Q_1 \\
 P_2 \stackrel{\text{def}}{=} a_2.b_2.P_2 & Q_2 \stackrel{\text{def}}{=} a_2.\bar{p}.b_2.\bar{v}.Q_2 \\
 & S \stackrel{\text{def}}{=} p.v.S \\
 X \stackrel{\text{def}}{=} P_1|P_2 & Y \stackrel{\text{def}}{=} (Q_1|Q_2|S) \setminus \{p, v\}
 \end{array}$$

Does it hold that  $X \sim Y$ ? Can  $X$  simulate  $Y$  and vice versa?

### Homework (not mandatory)

1. Point the pairs of processes that are in the bisimulation equivalence relation for any  $P, Q, R$ ? If you claim that the processes are not bisimilar, present a counterexample (define  $P, Q$  and  $R$  for which the relation does not hold):

$$\begin{array}{l}
 (P + Q) + R \sim P + (Q + R) ? \\
 a.(P + Q) \sim a.P + a.Q ? \\
 a.\tau.P \sim a.P ? \\
 P + \tau.Q \sim P + Q ? \\
 P + \tau.\tau.P \sim P ?
 \end{array}$$