Spreadsheet As a Relational Database Engine

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ABSTRACT

Spreadsheets are among the most commonly used applications for data management and analysis. Perhaps they are even among the most widely used computer applications of all kinds. However, the spreadsheet paradigm of computation still lacks sufficient analysis.

In this paper we demonstrate that a spreadsheet can play the role of a relational database engine, without any use of macros or built-in programming languages, merely by utilizing spreadsheet formulas. We achieve that by implementing all operators of relational algebra by means of spreadsheet functions.

Given a definition of a database in SQL, it is therefore possible to construct a spreadsheet workbook with empty worksheets for data tables and worksheets filled with formulas for queries. From then on, when the user enters, alters or deletes data in the data worksheets, the formulas in query worksheets automatically compute the actual results of the queries. Thus, the spreadsheet serves as data storage and executes SQL queries, and therefore acts as a relational database engine.

The paper is based on Microsoft Excel (TM), but our constructions work in other spreadsheet systems, too. We present a number of performance tests conducted in the beta version of Excel 2010. Their conclusion is that the performance is sufficient for a desktop database with a couple thousand rows.

Categories and Subject Descriptors

H.2.4 [Database Management]: Systems—relational databases; H.4.1 [Information Systems Applications]: Office Automation—spreadsheets

General Terms

Theory, Design, Performance

Keywords

spreadsheets, relational databases, relational algebra, SQL, performance

1. INTRODUCTION

Spreadsheets are the end-user computing counterpart of databases and OLAP in enterprise-scale computing. They serve basically the same purpose — data management and analysis, but at the opposite extremes of the data quantity scale.

At the same time spreadsheets are a great success, and are often described as the very first “killer app” for personal computers. Today they are used to manage home budgets, but also to create, manage and examine extremely sophisticated models and data arising in business and research. For example, Excel files are quite common as a form of supporting online material in Science journal.

It seems therefore surprising that relatively little research has been devoted to them and consequently they are still poorly understood. This is a source of many problems, e.g., Science provides an example of a scientific controversy [5, 3] which finally turned out to be related to the design of a spreadsheet used for data analysis. European Spreadsheet Risks Interest Group EuSpRIG http://www.eusprig.org with its annual conference are devoted to the problems with spreadsheets.

2. THE CONTRIBUTION

In this paper we aim at providing strong evidence, that spreadsheets are not only useful and successful, but also very interesting, and deserve more research. Specifically, we consider the relation of spreadsheets to database systems. It is a natural comparison, because spreadsheets indeed often play the role of small databases at the end-user level of computing.

We demonstrate that virtually any spreadsheet software present on the market is a relational database engine. We do so by implementing all operators of relational algebra using spreadsheet functions. For each query in SQL, we demonstrate how to construct a spreadsheet workbook with empty worksheets for data tables and worksheets filled with formulas for queries. As the user enters, alters or deletes data tuples in the data worksheets, the formulas in query worksheets automatically compute the actual results of the queries. Thus, the spreadsheet serves as data storage, and executes SQL queries. It is therefore a relational database engine. Consequently, any specification of a database, writ-
ten in SQL in the form of table and view definitions, can be compiled into a spreadsheet workbook which has exactly the same functionality as if the database was implemented in a classical RDBMS. Crucially, this is achieved without any use of macros written in an external programming language, like Visual Basic or the like. One might consider our construction also as an implementation of a relational database on a completely new type of (virtual) hardware.

As a model of spreadsheet syntax and semantics we take Microsoft Excel (TM) (the general reference is [10]), but our constructions work in other similar systems, like OpenOffice Calc, gnumeric or Google docs, too.

We present number of performance tests, which indicate that our constructions are efficient enough to be practically used as a desktop database storing a few thousand rows of data.

2.1 Application scenarios

We believe that there is a market niche for a small SQL database implemented in a spreadsheet. It is a low-end solution, in terms of performance. However, there is market for low-end mobile phones, for low-end computers, and similarly there is also market for low-end database solutions.

E.g., Chrome OS does not permit installing new applications. For a user of a netbook with this system, a method to have a small SQL database is to use our solution with the Google docs spreadsheet. This might be facilitated by a public "query compiler" in WWW, where the user types in SQL code and gets a couple of spreadsheet formulas to a public "query compiler" in WWW, where the user types in SQL code and gets a couple of spreadsheet formulas to a public "query compiler" in WWW, where the user types in SQL code and gets a couple of spreadsheet formulas to

2.2 Related work

To the best of our knowledge, the problem of expressing relational algebra and SQL in spreadsheets has not been considered before in the setting we adopt here. The most similar to our work reported here are the following. The paper [9] proposes an extension of the set of spreadsheet functions by carefully designed database function, whereby the user can specify (and later execute) SQL queries in a spreadsheet-like style, one step at a time. These additional operators were executed by a classical database engine running in the background. Our contribution means that exactly the same functionality can be achieved by the spreadsheet itself. Two papers [14, 15] describe a project, later named Query by Excel to extend SQL by spreadsheet-inspired functionality, allowing the user to treat database tables as if they were located in a spreadsheet and define calculations over rows and columns by formulas resembling those found in spreadsheets. In the final paper [16] a spreadsheet interface is offered for specifying these calculations, which had to be specified in an SQL-like code in the earlier papers. The paper [8] describes a method to allow RDBMs to query data stored in spreadsheets.

There is also a number of papers which discuss various methods to support high-level design of spreadsheets, in particular [1, 2, 6, 7, 11, 12, 13, 17, 18]. Some of them consider spreadsheets from the functional programming perspective.

3. TECHNICALITIES

We assume the reader to be basically familiar with spreadsheets. The paper is written to make the solutions compatible with Microsoft Excel (TM) 2003 version. The newest (at the time of this writing) Excel 2007 and beta 2010 provide a number of new functions, which simplify some of the tasks, but are not present in other spreadsheet systems. Therefore we chose compatibility with the older version, but refer to and test the newer systems, as well.

3.1 R1C1 notation

We use the row-column R1C1-style addressing of cells and ranges, supported by Excel. This notation is easier to handle in a formal description, although in everyday practice the equivalent A1 notation is dominating. The key advantage of the R1C1 notation is that the meaning of the formula is independent of the cell in which it is located.

In the R1C1 notation, both rows and columns of worksheets are numbered by integers from 1 onward. For arbitrary nonzero integers $i$ and $j$ and nonzero natural numbers $m$, $n$ the following expressions are cell references in the R1C1 notation: $RmCn$, $R[i]Cm$, $RmC[j]$, $R[i]C[j]$, $RCm$, $RC[i]$, $RmC$, $R[i]C$.

The number after ‘R’ refers to the row number and the number after ‘C’ to the column number. If that number is missing, it means “same row (column)” as the cell in which this expression is used. A number written in square brackets is a relative reference and the cell to which this expression points should be determined by adding that number to the row (column) number of the present cell. Number without brackets is an absolute reference to a cell whose row (column) number is equal to that number. For example, $R[-1]C7$ denotes a cell which is in the row directly above the present one in column 7, while $RC[3]$ denotes a cell in the same row as the present one and 3 columns to the right. If $R$ or $C$ is itself omitted, the expression denotes the whole column or row (respectively), e.g., $C7$ is column number 7. For referencing cells in other worksheets, RC may also be used, and references the cell whose row and column numbers are equal to the address of the cell in which this expression is located.

3.2 IF function

IF is a conditional function in spreadsheets. The syntax is IF(condition, true_branch, false_branch). Its evaluation is lazy, i.e., after the condition is evaluated and yields
either TRUE or FALSE, only one of the branches is evaluated. It can be therefore used to protect functions from being applied to arguments of wrong types, trap errors, and, last but not least, to speed up execution of queries by avoiding computing certain branches.

3.3 SUMPRODUCT function

We will often use a special function called SUMPRODUCT. Its uses will be generally modifications of the following two examples.

Example 1.

\[ \text{SUMPRODUCT}((\text{R1C1:R5C1=R1C3})*(\text{R1C2:R5C2=R1C4})) \]

is calculated as follows:

(i) each cell in the range R1C1:R5C1 is compared with R1C3, and this yields a sequence of five booleans;

(ii) each cell in the range R1C2:R5C2 is compared with R1C4, and this yields another sequence of five booleans;

(iii) the two sequences from previous items are multiplied coordinate-wise, which results in automatic data type conversion from booleans to integers, and then normal multiplication;

(iv) the five numbers are summed to give a single number as a result.

Consequently, the final result is the count of rows, in which the columns C1 and C2 contain the same pair of numbers as in R1C3:R1C4.

Example 2.

\[ \text{SUMPRODUCT}((\text{R1C1:R5C1=R1C3})*(\text{R1C2:R5C2=R1C4})*(\text{R1C5:R5C5})) \]

is calculated as follows:

(i-iii) the first three steps of evaluation are the same as before;

(iv) the sequence of 0s and 1s from the previous item and the range R1C5:R5C5 are multiplied again coordinate-wise, which results in a sequence of five numbers;

(v) again the sum of the above five numbers is returned.

The result is the sum of values in C5, calculated over those rows, in which the columns C1 and C2 contain the same pair of numbers as in R1C3:R1C4.

These two examples generalize to sum-multiplication of more than two or three arrays.

3.4 MATCH and INDEX functions

We use MATCH with syntax MATCH(range,cell,0). It returns the relative position of the first value in range which is equal to the value in cell, and error if that value does not appear there.

In one case we use MATCH(range,cell,1), in which case for range sorted into ascending order MATCH returns the relative position of the largest value in range that is less than or equal to the value in cell. We do not apply this form to unsorted ranges.

INDEX is used in the following syntax: INDEX(range,cell), and returns the value from range whose relative position is given by the value from cell.

3.5 Syntax variants

We will be using the SUMPRODUCT function with whole-column ranges, e.g., \( \text{SUMPRODUCT}((C1=R1C3)\times(C2=R1C4)) \), which is generally equivalent to the formula from Example 1, if no other values are present in columns C1 and C2. However, this syntax is not valid in Excel versions prior to 2007. In early Excel's one would have to use ranges like R1C1:Rmax in SUMPRODUCT, where max is the maximal row number of the range. OpenOffice Calc generally disallows R1C1 syntax and whole columns in formulas. Gnumeric and Google docs in turn permit both.

Our formulas are designed to work in all above systems, but in some of them they require syntactical modifications, mainly switching to A1 and eliminating whole-column ranges.

In Excel 2007 and 2010 there are new functions COUNTIFS and SUMIFS, which can substitute SUMPRODUCT in our applications, and are much more efficient. E.g., the first of our example formulas can be replaced by

\[ \text{COUNTIFS(R1C1:R5C1,R1C3,R1C2:R5C2,R1C4)} \]

and the second by

\[ \text{SUMIFS(R1C5:R5C5,R1C1:R5C1,R1C3,R1C2:R5C2,R1C4)} \].

4. ARCHITECTURE OF A DATABASE IMPLEMENTED IN A SPREADSHEET

In this paper, we disregard a number of minor issues arising in practical implementation of database operations in a spreadsheet. First of all, there is the obvious limitation of size on then number and sizes of relations, views and
their intermediate results, imposed by the maximal available number of worksheets, columns and rows in the spreadsheet system at hand. Next, the size of the data values (integers, strings, etc.) is also limited. The variety of data types in spreadsheets is also restricted when compared to database systems.

The overall architecture of a relational database implemented in a spreadsheet is as follows.

Given specification of the database, an implementation of a database is created by an external program (which plays the role of query compiler), in the form of an .xls, .xlsx, .odc, etc., file.

The whole resulting database is a workbook, consisting of one worksheet per data table and one worksheet per view in the database.

The data table worksheets are where the data is entered, updated and deleted. In the case of the (more theoretical in flavor) implementation of the relational algebra, the data table sheets do not contain any formulas and are simply the place to enter tuples into relations. In the case of SQL implementation, the cells are equipped with data validation formulas, which perform data type verification, enforce PRIMARY KEY, FOREIGN KEY and other integrity constraints included in the CREATE TABLE statements.

The query (view) worksheets are not supposed to be edited by the user. They contain columns filled with formulas, which calculate the consecutive values of the result of the query. Besides the result columns of the query, the view worksheets can also contain a number of hidden columns, which calculate and store intermediate results emerging during query evaluation. It is important that the formulas are completely uniform in each column of the database workbook, and they do not depend on the data which will be stored in the application. Initially all formulas compute the empty string "" value, representing unused space. When the user manually enters data into the tables, the automatic recomputation of the spreadsheet causes the results of queries to be computed and appear in the view worksheets.

5. THEORETICAL LEVEL: RELATIONAL ALGEBRA

We assume the semantics over a fixed domain of (the spreadsheet’s implementation of) integers, so that a relation is a set or multiset of tuples over the integers that are implemented in the spreadsheet software.

5.1 Compositionality

We assume the unnamed syntax for the relational algebra: relations and queries have columns, which are numbered and do not have any names. Sometimes we consider the expressions \( C_1, C_2, \ldots \), as the names of the worksheet columns, as well as the names of the columns in relations.

The representation of a relation \( r \) of arity \( n \) is a group of \( n \) consecutive columns in a worksheet, whose rows contain the tuples in the relation. The rows in which there are no tuples of \( r \) are assumed to be filled with the empty string formula """, evaluating to the empty string value "", which the user can replace by the new tuples of the relation. The empty string is never a component of a tuple in a relation or query. Therefore either all cells in a row contain the empty string, or none does. The rows of tables and queries evaluating to empty strings are called null rows henceforth.

The assumption that "" formulas fill the empty rows of data tables is only for uniformity of presentation. A formula in a cell can not evaluate to "empty cell" (because the formula occupies that cell anyway), only to empty string.

Therefore, if blank cells were used in empty rows, formulas expressing queries would have to be adapted to accept unused space in two different forms: empty cells in data tables, and empty strings in results of other queries.

The representation of a relational algebra query \( Q \) of arity \( m \) is a group of \( l + m \) consecutive columns in a worksheet. Initial segments of all its rows are filled with formulas (identical in all cells of each column), which calculate the tuples in \( Q \). We assume that the formulas in the last \( m \) columns should return either (a component of) a tuple in the result of \( Q \), or the empty string value "". The additional \( l \) columns are also filled with identical formulas, which calculate intermediate results. A worksheet of this kind can be created by entering the formulas in the first row, and then filling them downward to span as many rows as necessary. This uniformity assumption means in particular, that the formulas are completely independent of the data they will work on. However, we would like to stress that there is no reason to reject nonuniform implementations, should they prove to be more effective or permit expressing queries inexpressible in a uniform way.

In the following we will consider both set and bag (multiset) semantics of the relational algebra. In the first case, duplicate rows are not permitted in the relations and queries; in the latter they are permitted. However, even in the set semantics a spreadsheet representation of a relation may contain many null rows.

Furthermore, the representation may be loose if null rows are interspersed with the tuples, or standard if all the tuples come first, followed by the null rows.

Consequently, we have loose-set, loose-bag, standard-set and standard-bag semantics. No matter which of the above semantics we have in mind, the result of the query appears exactly as if it were a table, and can be used as such. Now the only thing necessary to compose queries is to locate their implementations side by side in a single worksheet and change input column numbers in the formulas computing the outermost query, to agree with the column numbers of the outputs of the argument queries (and then the output columns of the argument queries become the intermediate results columns of the composition).

Therefore, queries represented in this way are compositional.

Now it suffices to demonstrate that the each of the following relational algebra operators from [4] can be implemented in a spreadsheet:

- Two operations specific to spreadsheets, absent in [4]: error trapping and standardization (converting to standard form).
- Sorting.
- Duplicate removal \( \delta r \).
- Selection \( \sigma_{\theta} r \).
- Projection \( \pi_{i,j,\ldots} r \).
- Union \( r \cup s \).
- Difference \( r \setminus s \).
• Cartesian product \( r \times s \).
• Grouping with aggregation \( \gamma_{\theta} r \), where \( L \) is one of: \text{SUM}, \text{COUNT}, \text{AVG}, \text{MAX} \ and \text{MIN}.

5.2 Notation

We present here implementations based on spreadsheet functions which are common to most of (or even all) spreadsheet systems. This way we believe to consider the spreadsheet paradigm, even if its definition is not yet formulated in the literature.

We use the following convention for presenting implementations:

\[ \text{COLUMN} < = \text{FORMULA} \]

means that \text{FORMULA} is entered into each cell of the \text{COLUMN}, which may be specified either to be a single column (e.g. C5) or a range of a few columns (e.g. C5:C7), or a single cell (e.g. R1C5), and in each case belongs to the columns with intermediate values. The notation

\[ \text{COLUMN} < = \text{FORMULA} \]

indicates that formulas located in \text{COLUMN} calculate the output of the query.

Sometimes the output columns are not specified, and then it is always indicated, that the final output is computed by applying another, already defined operation to some of the columns with intermediate results. At two occasions we even write SQL queries as contents of spreadsheet columns, understanding that the spreadsheet formulas implementing them are written there.

Generally, we assume the arguments of the algebra operators to be two- or three-ary relations or queries, the generalization to higher arities is straightforward.

Except for the standardization and sorting, in all other cases we assume the input to be in the standard form, i.e., null rows at the bottom.

5.3 Error trapping and standardization

In this section we describe two special purpose operators, which perform common and useful tasks, specific to our spreadsheet environment.

5.3.1 Error trapping

If we replace a formula \( =F \), which may produce an error, by the formula \( =I\text{F} (=\text{ERROR}(F),**,F) \), any error produced by \( =F \) is replaced by the empty string, and otherwise the value is the same as the value of \( =F \).

5.3.2 Standardization

This operation converts a relation from loose to standard form, moving null rows to the bottom. The relative order of non-null rows is preserved. We assume that columns C1 and C2 contain the source data.

\[ \text{C3} < = \text{SUMPRODUCT}((\text{C1}<\text{RC1})*1) \]

counts the non-null rows above the present row, including the present one. This number is the row number to which the present row should be relocated. Note that multiplication by 1 enforces boolean to integer conversion.

\[ \text{C4} < = \text{MATCH}((\text{RCW}(),\text{C3},0) \]

returns the position of the first value in C3 equal to the present row number. If no match is found (i.e., we are in a row whose number is higher than the total number of non-null rows), an error is returned.

\[ \text{C5:C6} < = I\text{F}(=\text{ERROR}(\text{RC4}),**,\text{INDEX}([C[-4],\text{RC4}])) \]

Errors are trapped, and when there is no error, \text{INDEX} returns the data from the suitable row of C[4]. This puts in RiC3 the number of entries in column C1 which are smaller than or equal to RiC1. ** compared by \( = \) is larger than any number, so null rows do not give any errors, and in the following are treated as the largest entries.

\[ \text{C4} < = \text{RC3-SUMPRODUCT}((\text{C1}<\text{RC1})*1)+1 \]

This puts in RiC4 the number of entries in column C1 which are either smaller than RiC1 or equal to it and located in the same row or above it. This is the number of the row into which RiC1 should be relocated during sort.

\[ \text{C5:C6} < = \text{INDEX}([C[-4],\text{MATCH}((\text{ROW}()),\text{C4},0)) \]

This part is very similar to the standardization solution, except that there are no errors to be trapped and we combine two formulas into one.

Sorting in descending order is done by reverting the signs of numbers by the formula \( =I\text{F} (=\text{RC[-1]}==**;**;=-\text{RC[-1]} \) and sorting into ascending order, and then reverting the signs again. This leaves the null rows at the bottom. In particular, if sorting is necessary there is no need to standardize first.

An important property of this operation is that rows with empty string in the column on which the sort is performed, are moved to the bottom. Consequently, sorting brings any query or relation to standard form. Moreover, this form of sorting is stable.

5.5 Duplicate removal

Next we describe the implementation of duplicate removal, which, among other things, converts its input data from bag to set semantics. We assume the table to contain two columns C1:C2.

\[ \text{C3} < = \text{SUMPRODUCT}((\text{C1}=\text{RC1})*(\text{C2}=\text{RC2})) \]

This causes RiC3 to contain the number of tuples from C1:C2 which are equal to RiC1:RiC2 and are located at the same level or above it. This number is 1 iff the row contains the first occurrence of this tuple.

\[ \text{C4:C5} < = I\text{F}(=\text{RC3}=1,=\text{RC[-3]},**) \]

Now the first occurrences of tuples are copied into C4:C5, the other are replaced by null rows.

5.6 Selection

Assume that we are given a relation \( r \) located in C1:C2 and we want to compute \( \sigma_{\theta} r \), where \( \theta \) is a boolean combination of equalities and inequalities concerning the values of columns of \( r \) and constants. Then we use a spreadsheet formula expressing \( \theta \) to substitute ** for the rows which do not satisfy \( \theta \). This is best explained on an example: if \( \theta \)
is \((C1 \leq 100 \land C2 > C1) \lor C2 \neq 175\), then the selection is implemented by
\[
C3:C4 \leftarrow \text{IF}(\text{AND}(C1=100, C2>C1), \\
\text{RC2>175}, \text{RC}-2, \""
\]
It leaves the result of the selection in a loose (set or bag, inherited from the input) form.

5.7 Projection
The case of projection is quite easy: it amounts to omitting some columns from the input relation/query.

5.8 Union
Assume that we are given two relations located in \(C1:C2\) and \(C3:C4\), respectively.
Then use the following formulas to calculate their union in standard bag form.
\[
R1C5 < = \text{COUNT}(C1)
\]
\[
R2C5 < = \text{COUNT}(C3)
\]

We calculate the numbers of non-null rows in \(C1:C2\) and \(C3:C4\).
\[
C6:C7 \leftarrow \text{IF}(\text{ROW}()<R1C5*R2C5, \text{INDEX(C[-5]}, \\
\text{POLY((ROW()-1)/R2C5+1)}, \""
\]
If the present row number is less than \(R1C5\) then we take the same row from \(C1:C2\), otherwise we take rows from \(C3:C4\) whose numbers are suitably shifted. Note that this assumes the inputs to be in standard (set or bag) form.

5.9 Difference
Assume that we are given two relations located in \(C1:C2\) and \(C3:C4\), respectively. Then use the following formulas to calculate their set difference.
\[
C5 < = \text{SUMPRODUCT}((C3=RC1)*(C4=RC2))
\]
This calculates in \(R1C5\) the number of times a tuple equal to \(RiC1:RiC2\) appears in \(C3:C4\).
\[
C6:C7 \leftarrow \text{IF}(RC5=0, RC[-5], \""
\]
Now if \(R1C5\) is 0, we copy the row \(RiC1:RiC2\) to the output, otherwise we replace it by a null row.
The set/bag form of the result is inherited from the inputs. However, this construction does not work for the bag format, since in this case we should count the copies of identical rows in both relations and put in the output a suitable number of such rows.
The more complicated construction which does work is as follows:
\[
C5 < = \text{SUMPRODUCT}((C3=RC1)*(C4=RC2))
\]
This, exactly as before, calculates in \(R1C5\) the number of times a tuple equal to \(RiC1:RiC2\) appears in \(C3:C4\).
\[
C6:C7 \leftarrow \text{IF}(RC5>0, RC6, \"\", RC[-6])
\]
Now we replace by null rows the first \(R1C5\) occurrences of tuple \(RiC1:RiC2\), and leave unaffected the remaining ones, which gives the desired bag difference. The resulting relation is loose.

5.10 Cartesian product
Assume that two relations are located in \(C1:C2\) and \(C3:C4\), respectively.

Then use the following formulas to calculate their Cartesian product. The construction below works only for relations in standard form, otherwise standardization is necessary first.
\[
R1C5 < = \text{COUNT}(C1)
\]
\[
R2C5 < = \text{COUNT}(C3)
\]
We calculate the numbers of non-null rows in \(C1:C2\) and \(C3:C4\).
\[
C6:C7 \leftarrow \text{IF}(\text{ROW}()<=R1C5*R2C5, \text{INDEX(C[-5]}, \\
\text{POLY((ROW()-1)/R2C5+1)}, \""
\]
Creates \(R1C5\) blocks, the \(i\)-th block being \(R2C5\) copies of \(RiC1:RiC2\).
\[
C8:C9 \leftarrow \text{IF}(\text{ROW}()<=R1C5*R2C5, \text{INDEX(C[-5]}, \\
\text{POLY((ROW()-1), R2C5)+1), \""
\]
Repeats in circular fashion the consecutive rows of \(C3:C4\) a total of \(R1C5\) rounds.
Note that in this case, the set or bag form of the initial relations is inherited by their product.

5.11 Grouping with aggregation
In the following, we assume always the relation to be located in \(C1:C3\), grouping done over \(C1:C2\) and aggregation over \(C3\).

5.11.1 GROUP BY with SUM,COUNT and AVG
\[
C4 < = \text{SUMPRODUCT}((C1=RC1)*(C2=RC2)*C3)
\]
This array formula computes in \(R1C4\) the sum of all \(RjC3\) over all \(j\) such that \(RjC1:RjC2\) is equal to \(RiC1:RiC2\). Now we do duplicate elimination over \(C1:C2\) and \(C4\) and that is the desired result. Alternatively, with
\[
C4 < = \text{SUMPRODUCT}((C1=RC1)*(C2=RC2))
\]
we get the count instead of sum aggregation.
For average one has to compute GROUP BY with SUM and COUNT side-by-side and return the copy of \(C1:C2\) plus the sum column divided by the count column.

5.11.2 GROUP BY with MAX and MIN
Let us consider MAX, the other being handled symmetrically. First, the whole relation is sorted into descending order by \(C3\). On the result, elimination of duplicates is performed, which considers two rows identical when they agree on \(C1:C2\). Our implementation of this operation eliminates all occurrences of a tuple except the very first one. The one left is therefore accompanied by the maximal value of \(C3\), as desired.

5.12 Additional operators
Although semijoin and join are not on the list of algebra operators, they are extremely inefficient if implemented as a selection of a Cartesian product. Therefore we present more effective implementations of equijoin and equijoin.

5.12.1 Semijoin
Assume that we are given two relations located in \(C1:C2\) and \(C3:C4\), respectively, and we wish to compute the equijoin \(C1 : C2 \times_{C3=C4} C2 : C3\). This is achieved in the following way. The formulas
\[
C5 < = \text{IF}(\text{ISERROR(MATCH(RC1,C3,0)), \"\", RC1)}
\]
\[
C6 < = \text{IF}(RC5=\"\", \"\", RC2)
\]
empty the rows from \(C1:C2\) which do not belong to the semijoin. The resulting relation is loose.
5.12.2 Join

Let two relations be located in C1:C2 and C3:C4, respectively, and the equijoin C1:C2 ⋉ C3:C4 should be computed.

We distinguish two cases here. First, that the tables C1:C2 and C3:C4 represent a many-to-many relationship. The second, that C3 is a foreign key for C1:C2, so the relation is many-to-one. The former is much more general, the latter is much more frequent in normalized databases.

Many-to-many.

Our implementation utilizes a kind of index on the data tables. It is assumed that the tables are sorted on the C1 and C3 columns, respectively. Then let us use the following formulas:

\[
C5:C6 = \text{SELECT C1,COUNT(*) FROM C1:C2 GROUP BY C1}
\]

\[
C7 = \text{IF(RC5="",","",INDEX(C16,RC20)+C22)}
\]

\[
R1C7 = \text{IF(RC5="",","",1)}
\]

The last two lines should be understood that we first fill the whole column C7 with formulas, and then change the formula in its first cell. The columns C5:C7 provide the index, where each key from C1 is associated with its number of occurrences and the location of its first occurrence in this column. An analogous index for C3:C4 is created in columns C8:C10.

Now we create standardized semijoins

\[
C11:C13 = C5:C7 < C5=C6=C8
\]

\[
C14:C16 = C8 < C10 < C8<C10 C5
\]

which eliminate the elements from the index which will not appear in the join. The next steps are

\[
C17 = \text{IF(RC11="",","",INDEX(C12,RC15))}
\]

\[
\]

\[
R1C18 = 0
\]

\[
R1C19 = \text{MAX(C18)}
\]

The values in C17 are the sizes of the fragments of the join, corresponding to the consecutive values of the columns on which the join is computed. C18 contains the numbers of rows at which they should begin minus 1. Finally, R1C19 contains the cardinality of the join. Finally,

\[
C20 = \text{IF(RD(R1C19,"",MATCH(RD(R1C19,"",1),1))}
\]

\[
C21 = \text{IF(RC20="",","",INDEX(C12,RC20))}
\]

\[
R1C21 = \text{IF(RC20="",",0)}
\]

\[
C22 = \text{IF(RC20="",",INDEX(C11,RC20))}
\]

\[
C23 = \text{IF(RC20="",",INDEX(C12,C13,RC20)+INT(RC21,INDEX(C12,RC20)))}
\]

\[
C24 = \text{IF(RC20="",",INDEX(C4,INDEX(C16,RC20)+MOD(RC21,INDEX(C12,RC20))))}
\]

compute the join doing Cartesian products of fragments of initial tables corresponding to the same entries in the indexes.

In C20 function MATCH is used with the last parameter 1 to do inexact search for the fragment of the initial tables from which the tuple in join should originate (see section 3.4).

In C21 the consecutive numbers of rows with the same value of the key are calculated using dynamic programming rather than aggregation.

In C23:C24 the natural two-level addressing using nested INDEX functions is employed, but otherwise the formulas resemble those used for Cartesian product above.

Many-to-one.

In the following solution MATCH finds the position of the foreign key and INDEX fetches the tuple from that row.

\[
C5:C6 = \text{IF(RC1="",",RC[-4])}
\]

\[
C7:C8 = \text{IF(RC1="",",INDEX(C[-3],MATCH(RC1,C3,0))}
\]

6. PRACTICAL LEVEL: SQL

This part is devoted to the discussion of the implementation issues of SQL-92. It is less detailed than the previous section, and is more dependent on the particular properties of Excel.

Of the three parts of SQL: DDL, DML and DCL, that last one is irrelevant, since we construct a database for a single user.

6.1 NULL values

NULLs can be represented simply by the string NULL and handled as such. This is not difficult, but rather tedious, since all the formulas, whether implementing DDL or DML statements, must be adjusted to handle NULLs by introducing conditional IFs which test if the argument is a NULL and invoke either a special treatment of NULL or the standard formula for non-NULLs.

6.2 DDL

Let’s discuss DDL, i.e., mainly CREATE TABLE statements. We adopt the option to distinguish the data table from its input area. So for each CREATE TABLE statement we create a separate data table and a separate input table. The latter is indeed a query table (see below for details), which filters tuples which do not satisfy integrity constraints included in the DDL statement and displays a warning message for the user. The former then fetches the rows which satisfy the integrity constraints (by merely looking if there is a warning message or not), and does standardization.

We assume the user enters data elements adding them at the bottom. If elements are removed (simply using the DEL key), no new elements are added at their positions. Updates are performed by removing the old version of the tuple and immediately adding a new one at the bottom.

Function TYPE allows one to distinguish text, booleans and numbers, which, together with length function LEN for strings and inequalities for numbers allow one to enforce data type declarations. There are a few limitations to this rule, e.g., the empty string "" plays a special role in our implementation of relational algebra operators, and so does the string "NULL", which imposes a (mild) restriction on what kind of strings can be used. For the DATE statement, however, one has to use formatting, instead, which enforces numbers to be interpreted and displayed as dates.

UNIQUE and PRIMARY KEY are enforced by the duplicate elimination operator described above, which rejects tuples which have already appeared before.

FOREIGN KEY statements are enforced by a semijoin query. It does not seem that there is an easy method to implement policies concerning behavior of the database when one deletes a foreign key for a tuple, except the CASCADE option. This one is completely automatic: when the foreign key disappears, the tuples which reference it become illegal and disappear from the data table (because the formulas which transfer them to the data table return "" in the absence of
the foreign key), even though they remain in the input table (where a warning appears).

Concerning INDEX, we have already presented a kind of index in our implementation of equijoin.

Example 3. Let us consider the following DDL statement:

CREATE TABLE Ord(
  Id INT UNSIGNED NOT NULL PRIMARY KEY,
  ModelID INT NOT NULL REFERENCES Models (ModelID),
  Version SMALLINT,
  ModelDescr VARCHAR(40));

We assume the following:

- the input worksheet for the above table is OrdInput, and the worksheet of the data table is OrdData;
- worksheet ModelsData keeps in column C1 the primary key referenced to above;
- size limits for INT and SMALLINT are M and N, respectively;
- the limit for the number of rows in data tables is max.

The following formula is placed in column C5:

=IF(AND(RC1="",RC2="",RC3="",RC4=""),"", IF(OR(RC1="",RC2="",RC3="",RC4=""),"", "Invalid data"), IF(AND( IF(TYPE(RC1)=1,INT(RC1)=RC1,FALSE), RC1>=0,RC1<=M, COUNTIF(RC1:RC1,RC1)=1, COUNTIF(ModelsData!C1,RC2)=1, IF(TYPE(RC3)=1, AND(IN(TRC3)=RC3,ABS(RC3)<=N), RC3="NULL"), TYPE(RC4)=2,LEN(RC4)<=40), "", "Invalid data")))

The formula is a big IF, which behaves as follows: it returns an empty string (numbers in parentheses refer to the lines in the formula above): when the row is a null row (1), and otherwise an error message if at least one (but not all) of its fields is "" (2), and otherwise again "" if all of the following conditions hold:

(5-6) The first column contains a number whose integer part is equal to itself, is nonnegative and does not exceed M (note that we used IF – due to its lazy evaluation INT is never applied to non-numbers and does not give any error message).

(7) RC1 appears for the first time in its column.

(8) RC2 appears exactly once in the table ModelsData in the first column (assumed to contain the primary key of that relation) and in this branch of the initial IFs it is not "". Note that it is not necessary to verify that RC2 is a nonnegative integer in the specified range, because it is enforced in the foreign key table, so the count takes care of it.

(9-11) If RC3 is a number then it must be an integer whose absolute value does not exceed N, and if not number, then it is "NULL".

(12) RC4 is a text, whose length is in the specified range. Function LEN accepts numbers as inputs, so there is no need to protect it by IF.

Then the OrdData worksheet contains formulas

=IF(OrdInput!RC5="Invalid data","",OrdInput!RC)

in all its four columns. This gives a possibly loose data table, which can be standardized, if desired.

As it can be seen from the example, the actual translation of the CREATE TABLE statements can be quite complicated. The main reason is that now we have many data types and some of the functions must be prevented from being applied to arguments of wrong type, NULLs may show up, etc.

6.3 Transactions

A database expressed as a spreadsheet in general cannot be accessed concurrently, hence there is no need of transactions for concurrency control. Transactions for recovery are supported in the following form: COMMIT is executed by saving the current state of the workbook, while ROLLBACK is done by re-reading the spreadsheet from disk. “Undo” (Ctrl-Z) offers a limited but easy to use form of ROLLBACK.

7. PERFORMANCE

Unfortunately, Excel and other spreadsheets have not been designed to serve as database engines, so we can not expect very good performance of our implementations. Formulas with ranges as arguments generally always do linear scans, and they are used in a linear number of cells. Recomputation of cells, whether invoked automatically or manually, always applies to all of them, so they produce quadratic algorithms. Of course, there are still possibilities to get some improvement (at least of the constants), by using dynamic algorithms, which compute the values in cells accessing only a few neighboring cells, or exploit the lazy evaluation of IF statements to prune the computation trees significantly. This area is largely unexplored, as the whole problem of optimization queries to be executed in a spreadsheet.

Apart from reducing the cost of operations, the other important possibility is to reduce recomputation. Namely, some of the systems (including Excel again) permit references not only to other worksheets, but to other workbooks (i.e., files), too. This gives the possibility to locate each query in a different file and open it only when it is necessary. It is then recomputed, but other queries are not. In particular, when working with data tables no queries need to be open. A similar solution is to work with tables and queries located in worksheets of one workbook, but with automatic recomputation turned off. Instead, as an act of computing a query, the user manually orders recomputation only of the currently active worksheet (Shift-F9 in Excel).

7.1 Tests

The tests reported below are not intended to give a complete account of the performance of our implementation of SQL in a spreadsheet, nor to suggest methods of optimization. Our main goal is to indicate that for the basic operations and a simple but already useful query it is possible to store and process a few thousand tuples reasonably fast, and thus that our solution has the potential of being useful in practice.

The experiments were conducted using beta version of Excel 2010 running on Intel(R) Core(TM)2 Duo CPU at 2.4GHz, on a laptop with 4 GB RAM and Windows XP Professional SP3. The testing procedures were programmed in VBA. In general, during computation of the queries we
Figure 2: Performance graph of standardization. Number of tuples in the table is given in thousands, the number of rows with formulas is always equal to the number of tuples.

Figure 3: Performance graph of sorting. Number of tuples given in thousands, number of rows with formulas is equal to the number of tuples.

Figure 4: Performance graph of duplicate elimination operator over a two-column table. There are 10000 rows of formulas in all cases, the number of tuples in the table is given in thousands. The graphs illustrate computation time for the solution with SUMPRODUCT (broken line) and for the solution with SUMIFS (solid line) in seconds.
Figure 5: Performance graph of bag difference operator for two tables of identical size. Number of tuples in the table is given in thousands, the number of rows with formulas is always equal to the number of tuples. Time for the solution with `SUMPRODUCT` (broken line) is given in minutes, time for the solution with `SUMIFS` (solid line) is given in seconds.

Figure 6: Performance graph of a many-to-many equijoin. The horizontal axis represents cardinality of the join in thousands, the vertical one computation time in seconds. The data points come for six experiments with 10000 or 20000 rows of formulas in the query table, and sizes of joined relations ranging from 300 to 1000.

Figure 7: Performance graph of a many-to-one equijoin. The worksheet consists of 50000 rows of formulas, number of tuples in the table is given in thousands, the size of the table with foreign key is 5000 tuples (solid line) or 10% of the number of tuples in the first table (broken line).
tested both cores of the processor were fully active, but it remains to be verified how to implement queries to achieve optimal scalability with the increasing number of cores and/or processors. The amount of available memory was never a problem.

Descriptions of the charts are generally informative enough, and the operations correspond to those already described above. Additional explanations are necessary in a few cases, which are treated below.

We do not claim the the findings of this section carry over to other spreadsheets systems.

### 7.1.1 Insertions, deletions, updates

In automatic recomputation mode Excel recomputes only those formulas, which refer to the cells which have changed. We tested the implementation of the `CREATE TABLE` statement described in Section 6.2, whose formulas do not refer to cells below in the same table, only to those which are above. Hence insertion (always at the bottom of the table) evaluates a single formula only and, according to our measurements, takes about 20 to 30 milliseconds, almost irrespectively of the size of the table. However, the cost of a deletion or an update depends on the position at which it is performed, as it causes recomputing of all formulas which are located below, too. This is illustrated on the chart. The table with foreign keys had 1000 rows in all tests.

### 7.1.2 Join

The unusual shape of the chart for many-to-many join has been chosen to illustrate the fact, that the computation time depends linearly on the size of the resulting join, and the other factors (sizes of the joined tables, size of the query table with formulas) are relatively insignificant.

### 7.2 SUMIFS vs. SUMPRODUCT

In two cases we tested the alternative implementations, using `SUMIFS` instead of `SUMPRODUCT` function. The results are clear: solutions with the former are reasonable, while formulas using the latter are extremely slow and generally impractical—on one of the charts, we had to use minutes instead of seconds to measure the length of the computation.
8. CONCLUSIONS, FURTHER RESEARCH

We have demonstrated that relational algebra can be naturally expressed in a spreadsheet, thus showing the power of the spreadsheet paradigm, which subsumes on the theoretical level the paradigm of relational databases. This can be understood as an implementation of a relational database on a completely new type of (virtual) hardware. Of course, in practice the effectiveness of this database is rather low, but our test demonstrate that it has the potential to be useful as an end-user desktop database with a few thousand rows of data.

The following problems questions seem worth exploring:

- Develop a methodology to optimize SQL queries executed in a spreadsheet.

- Can spreadsheets execute queries not expressible in SQL-92? In particular, can spreadsheets execute recursive queries, like those WITH . . . SELECT in SQL-99, or those in Datalog?

- Our implementations of SQL queries use uniform spreadsheets, in which all rows of a query table are identical. Could nonuniformity help in improving performance, or even allow expressing more queries?

- Can spreadsheets naturally implement other models of databases, like semi-structured or object-relational ones?

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10. REFERENCES


