

Idris

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Advanced Functional Programming

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Advanced functional programming

My part of the lecture:

theorem proving and programming with dependent types

Plan:

- Idris (1 lecture)
- Coq (6 lectures)
 - Coq project (grades)

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Motivation for dependent types: specifications

- types become more precise
- finer types better specify the properties of the function

Inductive *ftree* : *nat* → Set :=

| *Leaf* : *ftree* 0

| *Node* : ∀ *n* : *nat*, *Z* → *ftree* *n* → *ftree* *n* → *ftree* (*S* *n*).

Definition *root* (*n* : *nat*)(*t* : *ftree*(*S* *n*)) : *Z* :=

match *t* with

| *Node* *n* *k* | *r* ⇒ *k*

end.

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Dependent types - introduction

Functional dependent type - type of a function whose codomain depends on an argument

- $M : \text{Array } n$ means that M is an array of size n ,
- $\text{Array} : \text{nat} \rightarrow *$ is a type constructor,
- $\text{Zeroes } n : \text{Array } n$ is an array of n zeroes,
- mapping $n \mapsto \text{Zeroes } n$ has functional dependent type

$$\forall n : \text{nat}. \text{Array } n$$

Notations:

$$\forall n : \text{nat}. \text{ftree } n$$

$$\prod n : \text{nat}. \text{ftree } n$$

$$\text{forall } n : \text{nat}, \text{ftree } n$$

$$(n : \text{nat}) \rightarrow \text{ftree } n$$

Convention: $\text{forall } n : \text{nat}, \text{bool} \equiv \text{nat} \rightarrow \text{bool}$

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`forall n : nat, ftree n`

`(n : nat) → ftree n`

Convention: `forall n : nat, bool` \equiv `nat → bool`

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Dependencies in types

type List A depends on a type A (polimorphism)

type ftree n depends on a value n (dependent type)

type vector A n depends on a type A and value n (dependent type)

Dependent types - computations in types

`ftree (2+2) ≡ ftree (4)`

these types are *convertible* - should be regarded as internally equal

Attention:

for `+` defined by pattern matching on first argument:

`0 + y = y`

`(S x) + y = S (x+y)`

- `2+2` computes to `4`
- `0+n` computes to `n`
- but `n+0` does not compute to `n`
(equality can be proved by induction)

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Dependent types - in simplified Idris

```
data Parity : nat -> Type where
| Even : forall n:nat, Parity (n + n)
| Odd  : forall n:nat, Parity (S (n + n))
```

hence `Even i : Parity (i+i)` for a given `i : nat`

```
parity : (n:nat) -> Parity n
parity 0 = Even 0
parity (S 0) = Odd 0
parity (S (S k)) = match (parity k) with
| Even j => Even (S j)
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Type of `Even (S j)` is `Parity((S j) + (S j))`, but expected type is `Parity(S (S k))` where `k` is `j+j`.

Conclusion: we need a proof that `S (j+(S j))` equals `S (S (j+j))`

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- general purpose pure functional programming language with dependent types
- syntax similar to Haskell, but the meanings of `:` and `::` are interchanged
- type declarations required
- eager evaluation, lazy computations are possible
- dependent types
- types are first class language constructs (can be arguments to functions, returned from functions)
- dependent types provide better specifications of functions
- but writing a function that satisfies its specification may need proofs
- type-driven development treats programming as “solving a puzzle”: the program is the solution to the puzzle, the type is the goal of the puzzle
- because of dependent types, evaluation is needed at type-checking
- functions used in evaluation must be total and terminating
- compiler gets rid of the arguments to functions and constructors bound with quantity/multiplicity 0; erased arguments are still relevant at compile time.

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- general purpose pure functional programming language with dependent types
- syntax similar to Haskell, but the meanings of `:` and `::` are interchanged
- type declarations required
- eager evaluation, lazy computations are possible
- dependent types
- types are first class language constructs (can be arguments to functions, returned from functions)
- dependent types provide better specifications of functions
- but writing a function that satisfies its specification may need proofs
- type-driven development treats programming as “solving a puzzle”: the program is the solution to the puzzle, the type is the goal of the puzzle
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Idris - getting started

- installation: see <https://www.idris-lang.org/pages/download.html>
- `idris2 foo.idr` enters the interactive environment, similar to `ghci`
- commands, `:t`, `:q` (type `:?` for full list of commands)
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Idris and dependent types - examples

- Hello.idr
- Generic.idr
- Let_Where.idr
- FCTypes.idr
- Vectors.idr
- TCVects.idr
- WordLength_vec.idr
- ApplyVec.idr
- Adder.idr
- RemoveElem.idr
- Parity.idr
- Binary.idr
- AppendVecRew.idr

Interfaces

- similar to type classes in Haskell
- there can be many implementations for one type

(see Eq.idr Tree.idr)

Equality in Idris

- `==` is not adequate
- equality defined at the level of types

(see `EqNat.idr`, `ExactLength.idr`)

Totality checking

Function is *total* if it

- covers all possible inputs
- is well-founded (in recursive calls arguments are decreasing)
- does not use any data types which are not strictly positive
- does not call any non-total functions

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Allow to control

- linearity (used exactly once)
- erasure (not used at runtime)
- and unrestricted use.

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