Critical mass in a parabolic-elliptic Patlak-Keller-Segel equation with nonlinear diffusion

Philippe Laurençot¹, Adrien Blanchet and José Antonio Carillo

 $^1 \mathrm{Institut}$ de Mathematiques de Toulouse, Université Paul Sabatier

 ${}^1 \verb+laurenco@math.ups-tlse.fr$

For a specific choice of the (nonlinear) diffusion, there is a threshold mass in the parabolic-elliptic Patlak-Keller-Segel equation with nonlinear diffusion in space dimension greater or equal to three which separates initial data leading to global solutions and those blowing up in finite time, a situation reminiscent from the two-dimensional case with linear diffusion. There are however some new features such as the existence of integrable stationary solutions and backward self-similar solutions which will be discussed.