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{n > 0}
i := 1;
kw := 4;
while { $\gamma_1: kw = (2 * i)^2 \wedge i^2 \leq n \wedge \exists k \geq 0. i = 2^k$ }
  kw  $\leq$  n
do
  (i := 2*i;
  { $\alpha_1: kw = i^2 \wedge i^2 \leq n \wedge \exists k \geq 0. i = 2^k$ }
  kw := 4*kw
  )
{ $\alpha_2: kw = (2 * i)^2 \wedge i^2 \leq n < kw \wedge \exists k \geq 0. i = 2^k$ }
r := i;
dri := kw div2;
ik := dri div2;
{ $kw = (2 * i)^2 \wedge i^2 \leq n < kw \wedge ik = i^2 \wedge dri = 2 * r * i \wedge r = i \wedge \exists k \geq 0. i = 2^k$ }
while { $\gamma_2: kw = (r + i)^2 \wedge r^2 \leq n < kw \wedge ik = i^2 \wedge dri = 2 * r * i \wedge \exists k \geq 0. i = 2^k$ }
  i > 1
do
  (i := i div2;
  { $\alpha_3: kw = (r + 2 * i)^2 \wedge r^2 \leq n < kw \wedge ik = (2 * i)^2 \wedge dri = 2 * r * (2 * i) \wedge \exists k \geq 0. i = 2^k$ }
  ik := (ik div2) div2;
  { $kw = (r + 2 * i)^2 \wedge r^2 \leq n < kw \wedge ik = i^2 \wedge dri = 2 * r * (2 * i) \wedge \exists k \geq 0. i = 2^k$ }
  dri := dri div2;
  { $\alpha_4: kw = (r + 2 * i)^2 \wedge r^2 \leq n < kw \wedge ik = i^2 \wedge dri = 2 * r * i \wedge \exists k \geq 0. i = 2^k$ }
  if (kw - dri - 3*ik)  $\leq$  n
  then
    { $kw - dri - 3 * ik = (r + 2 * i)^2 - 2 * r * i - 3 * i^2 = (r + i)^2 \leq n \wedge$ 
       $kw = (r + 2 * i)^2 \wedge r^2 \leq n < kw \wedge ik = i^2 \wedge dri = 2 * r * i \wedge \exists k \geq 0. i = 2^k$ }
    r := r + i;
    { $\alpha_5: r^2 \leq n \wedge kw = (r + i)^2 \wedge n < kw \wedge ik = i^2 \wedge dri = 2 * (r - i) * i \wedge \exists k \geq 0. i = 2^k$ }
    dri := dri + 2*ik
    { $kw = (r + i)^2 \wedge r^2 \leq n < kw \wedge ik = i^2 \wedge dri = 2 * r * i \wedge \exists k \geq 0. i = 2^k$ }
  else
    { $kw - dri - 3 * ik = (r + 2 * i)^2 - 2 * r * i - 3 * i^2 = (r + i)^2 > n \wedge$ 
       $kw = (r + 2 * i)^2 \wedge r^2 \leq n < kw \wedge ik = i^2 \wedge dri = 2 * r * i \wedge \exists k \geq 0. i = 2^k$ }
    kw := kw - dri - 3*ik;
    { $kw = (r + i)^2 \wedge r^2 \leq n < kw \wedge ik = i^2 \wedge dri = 2 * r * i \wedge \exists k \geq 0. i = 2^k$ }
  )
{i  $\leq$  1  $\wedge kw = (r + i)^2 \wedge r^2 \leq n < kw \wedge ik = i^2 \wedge dri = 2 * r * i \wedge \exists k \geq 0. i = 2^k$ }
{ $r^2 \leq n < (r + 1)^2$ }

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